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NCERT Class 9 Solutions: Quadrilaterals (Chapter 8) Exercise 8.1 Part 5

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## Quadrilateral Classification Chapt

| §h2pe | Characteristic | N^2me |
| :---: | :---: | :---: |
|  | No parallel sides | Trapezium |
|  | Exactly one pair of parallel sides | Trapezoid |
|  | Two pairs of parallel sides | Parallelogram |
|  | Parallelogram with congruent sides | Rhombus |
|  | Parallelogram with right angles | Rectangle |
|  | Rectangle with congruent sides | Square |
| Note that squares, rectangles, and rhombuses are types of parallelograms and that a square is a type of rectangle and a type of rhombus. |  |  |

Q-9 In parallelogram ABCD , two points P and Q are taken on diagonal BD such that $D P=B Q$ (see Fig.) . Show that:

1. $\triangle A P D \cong \triangle C Q B$
2. $A P=C Q$
3. $\triangle A Q B \cong \triangle C P D$
4. $A Q=C P$
5. APCQ is a parallelogram


Solution:

1. In $\triangle \mathrm{APD}$ and $\triangle C Q B$,
2. $D P=B Q$ (Given)
3. $\angle A D P=\angle C B Q$ (Alternate interior angles)
4. $A D=B C$ (Opposite sides of a parallelogram)

Thus, $\triangle A P D \cong \triangle C Q B$ by Side-Angle-Side congruence condition.

1. $A P=C Q$ By Corresponding parts of congruent triangles as $\triangle A P D \cong \triangle C Q B$.
2. In $\triangle \mathrm{AQB}$ and $\triangle C P D$,
3. $B Q=D P$ (Given)
4. $\angle A B Q=\angle C D P$ (Alternate interior angles)
5. $\mathrm{AB}=\mathrm{CD}$ (Opposite sides of a parallelogram)

Thus, $\triangle \mathrm{AQB} \cong \triangle \mathrm{CPD}$ by Side-Angle-Side congruence condition.

1. $A Q=C P$ By Corresponding Parts of Congruent Triangles as $\triangle A Q B \cong \triangle C P D$.
2. The diagonal of a parallelogram bisect each other.
3. $O B+O D$
4. $O B-B Q=O D-D P \mid B Q=D P$ Given
5. $O Q=O P$... equation (1)

Also, $O A=O C$... equation (2) (diagonal of a parallelogram bisect each other)
From equation (1) and (2) , APCQ is parallelogram
Q-10 ABCD is a parallelogram and AP and CQ are perpendiculars from vertices $A$ and $C$ on on diagonal BD (see Fig.) . Show that

1. $\triangle A P B \cong \triangle C Q D$
2. $A P=C Q$


Solution:
Given,

- ABCD is parallelogram
- AP and CQ are perpendiculars from A and C on diagonal BD

Solution (i)
In $\triangle A P B$ and $\triangle C Q D$,

- $A B=C D$ (Opposite side of parallelogram ABCD)
- $\angle A B P=\angle C D Q$ (Alternate interior angles)
- $\therefore A B \| D C$

Now,

- $\angle A P B=\angle C Q D$ (Equal to right angles as AP and CQ are perpendiculars)
- $A B=C D(\mathrm{ABCD}$ is a parallelogram)
- Thus, $\triangle A P B \cong \triangle C Q D$ by Angle-Angle-Side congruence condition.

Solution (ii)
$A P=C Q$ by Corresponding Parts of Congruent Triangles as $\triangle A P B \cong \triangle C Q D$.

