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## Probability: Probability Definition in Math and Formula for Probability

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**Probability** means possibility. It is a branch of mathematics that deals with the occurrence of a random event. The value is expressed between zero and one. Probability has been introduced in Math's to predict how likely events are to happen.

The meaning of probability is basically the extent to which something is likely to happen. This is the basic probability theory, which is also used in the probability distribution, where you will learn the possibility of outcomes for a random experiment. To find the probability of a single event to occur, first we should know the total number of possible outcomes.

### Probability Definition in Math

Probability is a measure of the likelihood of an event to occur. Many events cannot be predicted with total certainty. We can predict only the chance of an event to occur i.e., how likely they are to happen, using it. Probability can range in between 0 to 1, where 0 means the event to be an impossible one and 1 indicates a certain event. Probability for class 10 is an important topic for the students which explains all the basic concepts of this topic. **The probability of all the events in a sample space sums up to 1.**

**For example**, when we toss a coin, either we get Head OR Tail, only two possible outcomes are possible (H, T) . But if we toss two coins in the air, there could be three possibilities of events to occur, such as both the coins show heads or both shows tails or one shows heads and one tail, i.e.,  $(H, H), (H, T), (T, T)$  .

### Formula for Probability

The probability formula is defined as the possibility of an event to happen is equal to the ratio of the number of favorable outcomes and the total number of outcomes.

$$\text{Probability of event to happen } P(E) = \frac{\text{Number of favourable outcomes}}{\text{Total number of Outcomes}}$$

Sometimes students get mistaken for “favorable outcome” with “desirable outcome.” This is the basic formula. But there are some more formulas for different situations or events.

### Examples and Solutions

**(1) There are 6 pillows in a bed, 3 are red, 2 are yellow and 1 is blue. What is the probability of picking a yellow pillow?**

Ans: The probability is equal to the number of yellow pillows in the bed divided by the total number of pillows, i.e.,  $\frac{2}{6} = \frac{1}{3}$ .

**(2) There is a container full of colored bottles, red, blue, green, and orange. Some of the bottles are picked out and displaced. Sumit did this 1000 times and got the following results:**

- No. of blue bottles picked out: 300
- No. of red bottles: 200
- No. of green bottles: 450
- No. of orange bottles: 50

**(a) What is the probability that Sumit will pick a green bottle?**

Ans: For every 1000 bottles picked out, 450 are green.

$$\text{Therefore, } P(\text{green}) = \frac{450}{1000} = 0.45$$

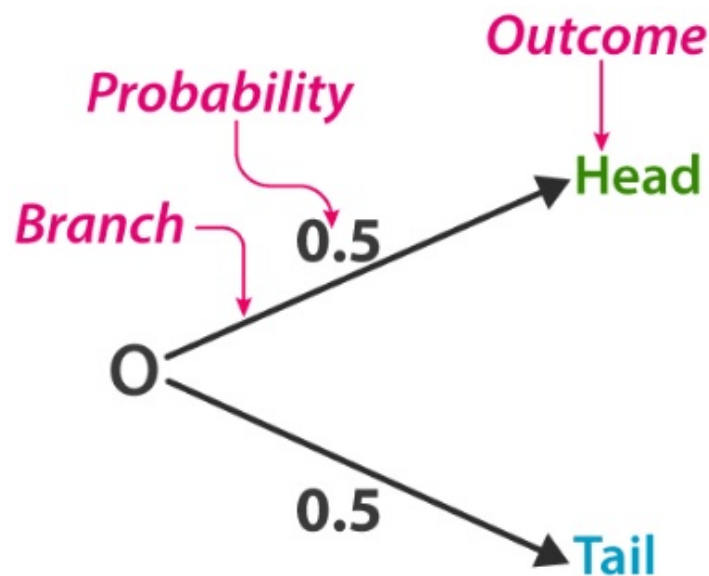
**(b) If there are 100 bottles in the container, how many of them are likely to be green?**

Ans: The experiment implies that 450 out of 1000 bottles are green.

Therefore, out of 100 bottles, 45 are green.

## Probability Tree

The **tree diagram** helps to organize and visualize the different possible outcomes. Branches and ends of the tree are two main positions. Probability of each branch is written on the branch, whereas the ends are containing the outcome. Tree diagram used to figure out when to multiply and when to add. You can see below a tree diagram for the coin:



## Types of Probability

There are three major types of probabilities:

- Theoretical Probability
- Experimental Probability
- Axiomatic Probability

### Theoretical Probability

It is based on the possible chances of something to happen. The theoretical probability is mainly based on the reasoning behind probability. For example, if a coin is tossed, the theoretical probability of getting head will be  $\frac{1}{2}$

### Experimental Probability

It is based based on the observations of an experiment. The experimental probability can be calculated based on the number of possible outcomes by the total number of trials. For example, if a coin is tossed 10 times and heads is recorded 6 times then, the experimental probability for heads is  $\frac{6}{10}$  or,  $\frac{3}{5}$ .

## Axiomatic Probability

In axiomatic probability, a set of rules or axioms are set which applies to all types. These axioms are set by Kolmogorov and are known as **Kolmogorov's three axioms**. With the axiomatic approach to probability, the chances of occurrence or non-occurrence of the events can be quantified. The axiomatic probability lesson covers this concept in detail with Kolmogorov's three rules (axioms) along with various examples.

Conditional Probability is the likelihood of an event or outcome occurring based on the occurrence of a previous event or outcome.

## Probability of an Event

Assume an event E can occur in r ways out of a sum of n probable or possible **equally likely ways**. Then the probability of happening of the event or its success is expressed as;

$$P(E) = \frac{r}{n}$$

The probability that the event will not occur or known as its failure is expressed as:

$$P(E') = n - \frac{r}{n} = 1 - \frac{r}{n}$$

E' represents that the event will not occur.

Therefore, now we can say,

$$P(E) + P(E') = 1$$

This means that the total of all the probabilities in any random test or experiment is equal to 1.

## What Are Equally Likely Events?

When the events have the same theoretical probability of happening, then they are called equally likely events. The results of a sample space are called equally likely if all of them have the same probability of occurring. For example, if you throw a die, then the probability of getting 1 is  $\frac{1}{6}$ .

Similarly, the probability of getting all the numbers from 2, 3, 4, 5 and 6, one at a time is  $\frac{1}{6}$ . Hence, the following are some examples of equally likely events when throwing a die:

- Getting 3 and 5 on throwing a die
- Getting an even number and an odd number on a die
- Getting 1, 2 or 3 on rolling a die

are equally likely events, since the probabilities of each event are equal?

## Complementary Events

The possibility that there will be only two outcomes which states that an event will occur or not. Like a person will come or not come to your house, getting a job, or not getting a job, etc. are examples of complementary events. Basically, the complement of an event occurring in the exact opposite that the probability of it is not occurring. Some more examples are:

- It will rain or not rain today
- The student will pass the exam or not pass.

- You win the lottery, or you don't.

**Also, read:**

- Independent Events
- Mutually Exclusive Events

Probability Density Function

The Probability Density Function (PDF) is the probability function which is represented for the density of a continuous random variable lying between a certain range of values. Probability Density Function explains the normal distribution and how mean and deviation exists. The standard normal distribution is used to create a database or statistics, which are often used in science to represent the real-valued variables, whose distribution are not known.

Probability Terms and Definition

Some of the important probability terms are discussed here:

Term	Definition	Example
Sample Space	The set of all the possible outcomes to occur in any trial	1. Tossing a coin, Sample Space $(S) = H, T$ 2. Rolling a die, Sample Space $(S) = 1, 2, 3, 4, 5, 6$
Sample Point	It is one of the possible results	In a deck of Cards: 4 of hearts is a sample point.  the queen of Clubs is a sample point.
Experiment or Trial	A series of actions where the outcomes are always uncertain.	The tossing of a coin, Selecting a card from a deck of cards, throwing a dice.
Event	It is a single outcome of an experiment.	Getting a Heads while tossing a coin is an event.
Outcome	Possible result of a trial/experiment	T (tail) is a possible outcome when a coin is tossed.
Complimentary event	The non-happening events. The complement of an event A is the event not A (or A')	Standard 52-card deck, $A =$ Draw a heart, then $A' =$ don't draw a heart
Impossible Event	The event cannot happen	In tossing a coin, impossible to get both head and tail

## Solved Probability Problems

**Question 1: Find the probability of rolling a '3 with a die.'**

**Solution:**

Sample Space = 1, 2, 3, 4, 5, 6

Number of favorable events = 1

Total number of outcomes = 6

Formula,

$$\text{Probability of event to happen } P(E) = \frac{\text{Number of favourable outcomes}}{\text{Total number of Outcomes}}$$

Put the value,

$$\text{Thus, Probability, } P = \frac{1}{6}$$

**Question 2: Draw a random card from a pack of cards. What is the probability that the card drawn is a face card?**

**Solution:**

A standard deck has 52 cards .

Total number of outcomes = 52

Number of favorable events =  $4 \times 3 = 12$  (considered Jack, Queen and King only)

Probability,

$$\begin{aligned} \text{Probability of event to happen } P(E) &= \frac{\text{Number of favourable outcomes}}{\text{Total number of Outcomes}} \\ &= \frac{12}{52} \\ &= \frac{3}{13} \end{aligned}$$

**Question 3: A vessel contains 4 blue balls, 5 red balls and 11 white balls. If three balls are drawn from the vessel at random, what is the probability that the first ball is red, the second ball is blue, and the third ball is white?**

Solution: The probability to get first ball is red or the first event is  $\frac{5}{20}$  .

Now, since we have drawn a ball for the first event to occur, then the number of possibilities left for the second event to occur is  $20 - 1 = 19$ .

Hence, the probability of getting second ball as blue or the second event is  $\frac{4}{19}$ .

Again, with the first and second event occurred, the number of possibilities left for the third event to occur is  $19 - 1 = 18$ .

And the probability of the third ball is white, or third event is  $\frac{11}{18}$ .

Therefore, the probability is  $\frac{5}{20} \times \frac{4}{19} \times \frac{11}{18} = \frac{44}{1368} = 0.032$ .

Or we can express it as  $P = 3.2\%$ .

**Question 4: Two dice are rolled, find the probability that the sum is:**

1. equal to 1
2. equal to 4
3. less than 13

Solution:

(1) To find the probability that the sum is equal to 1 we must first determine the sample space  $S$  of two dice as shown below.

$$S = (1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 6)$$

$$(2, 1), (2, 2), (2, 3), (2, 4), (2, 5), (2, 6)$$

$$(3, 1), (3, 2), (3, 3), (3, 4), (3, 5), (3, 6)$$

$$(4, 1), (4, 2), (4, 3), (4, 4), (4, 5), (4, 6)$$

$$(5, 1), (5, 2), (5, 3), (5, 4), (5, 5), (5, 6)$$

$$(6, 1), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6)\}$$

(1) Let  $E$  be the event "sum equal to 1". Since, there are no outcomes which where a sum is equal to 1, hence,

$$P(E) = \frac{n(E)}{n(S)} = \frac{0}{36} = 0$$

(2) Three possible outcomes give a sum equal to 4 such as;

$$E = (1, 3), (2, 2), (3, 1)$$

$$\text{Hence, } P(E) = \frac{n(E)}{n(S)} = \frac{3}{36} = \frac{1}{12}$$

3) From the sample space, we can see all possible outcomes,  $E = S$ , give a sum less than 13. Like:

(1, 1) or (1, 6) or (2, 6) or (6, 6). So, you can see the limit of an event to occur is when both dies have number 6, i.e., (6, 6). Hence,

$$P(E) = \frac{n(E)}{n(S)} = \frac{36}{36} = 1$$

Example: 5 In Class, 30% of the students offered English, 20% offered Hindi and 10% offered both. If a student is selected at random, what is the probability that he has offered English or Hindi?

Solution:

$$P(E) = \frac{30}{100} = \frac{3}{10}, P(H) = \frac{20}{100} = \frac{1}{5} \text{ and } P(E \cap H) = \frac{10}{100} = \frac{1}{10}$$

$$P(E \text{ or } H) = P(E \cup H)$$

$$= P(E) + P(H) - P(E \cap H) = \left( \frac{3}{10} + \frac{1}{5} - \frac{1}{10} \right) = \frac{4}{10} = \frac{2}{5}$$

## FAQs on Probability

### What is Probability? Give an Example

Probability is a branch of mathematics that deals with occurrence of a random event. For example, when a coin is tossed in the air, the possible outcomes are Head and Tail.

### What is the Formula of Probability?

The probability formula is defined as the possibility of an event to happen is equal to the ratio of the number of outcomes and the total number of outcomes.

### What Are the Different Types of Probability?

There are three major types of probabilities: Theoretical Probability, Experimental Probability, Axiomatic Probability

### What Are the Basic Rules of Probability?

If A and B are two events, then,

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) \quad P(A \cap B) = P(B) \cdot P(A|B)$$