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CBSE Class 10- Mathematics: Chapter – 8 Introduction to Trigonometry Part 1

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Introduction to Trigonometry

"The mathematician is fascinated with the marvelous beauty of the forms he constructs, and in their beauty he everlasting truth."

Question 1:

If $x\cos\theta - y\sin\theta = a$, $x\sin\theta + y\cos\theta = b$, prove that $x^2 + y^2 = a^2 + b^2$.

Answer:

$$x\cos\theta - y\sin\theta = a$$

$$x \sin \theta + y \cos \theta = b$$

Squaring and adding

$$x^2 + v^2 = a^2 + b^2$$
.

Question 2:

Prove that $\sec^2 \theta + \cos ec^2 \theta$ can never be less than 2.

Answer:

 $S.T \sec^2 \theta + \cos ec^2 \theta$ can never be less than 2.

If possible, let it be less than 2.

$$1 + Tan^2\theta + 1 + \cot^2\theta < 2$$
.

$$\Rightarrow$$
 2 + tan² θ + cot² θ

$$\Rightarrow (\tan \theta + \cot \theta) 2 < 2$$

Which is not possible.

Question 3:

If
$$\sin \varphi = \frac{1}{2}$$
, show that $3\cos \varphi - 4\cos^3 \varphi = 0$

Answer:

$$\sin \phi = \frac{1}{2}$$

$$\Rightarrow \phi = 30^{\circ}$$

Substituting in place of $\phi = 30^{\circ}$. We get .

Question 4:

If
$$\sin^2 \varphi + 3\cos^2 \varphi = 4S.T.$$
, show that $\tan \varphi = \frac{1}{\sqrt{3}}$

Answer:

If
$$7 \sin^2 \varphi + 3 \cos^2 \varphi = 4S.T.$$
, $\tan \varphi \frac{1}{\sqrt{3}}$

$$7 \sin^2 \varphi + 3 \cos^2 \varphi = 4 \left(\sin^2 \varphi + \cos^2 \varphi\right)$$

$$\Rightarrow 3 \sin^2 \varphi = \cos^2 \varphi$$

$$\Rightarrow \frac{\sin^2 \varphi}{\cos^2 \varphi} = \frac{1}{3}$$

$$\Rightarrow \tan^2 \varphi = \frac{1}{3}$$

$$\tan \varphi = \frac{1}{\sqrt{3}}$$

Question 5:

If $\cos \varphi + \sin \varphi = \sqrt{2} \cos \varphi$, prove that $\cos \varphi - \sin \varphi = \sqrt{2} \sin \varphi$

Answer:

$$\cos \varphi + \sin \varphi = \sqrt{2} \cos \varphi$$

$$\Rightarrow (\cos \varphi + \sin \varphi)^2 = 2 \cos^2 \varphi$$

$$\Rightarrow \cos^2 \varphi + \sin^2 \varphi + 2 \cos \varphi \sin \varphi = 2 \cos^2 \varphi$$

$$\Rightarrow \cos^2 \varphi - 2 \cos \varphi \sin \varphi + \sin^2 \varphi = 2 \sin^2 \varphi$$

$$\Rightarrow (\cos \varphi - \sin \varphi)^2 = 2 \sin^2 \varphi$$

$$\left[\therefore 2 \sin^2 \varphi = 2 - 2 \cos^2 \varphi \right]$$

$$1 - \cos^2 \varphi = \sin^2 \varphi & 1 - \sin^2 \varphi = \cos^2 \varphi$$

$$\cos \varphi - \sin \varphi = \sqrt{2} \sin \varphi.$$

Question 6:

If $\tan A + \sin A = m$ and $\tan A - \sin A = n$, show that $m^2 - n^2 = \sqrt{mn}$

Answer:

$$\tan A + \sin A = m \tan A - \sin A = n$$

$$m^2 - n^2 = \sqrt{mn}.$$

$$= m^2 - n^2 = (\tan A + \sin A)^2 - (\tan A - \sin A)^2$$

$$= 4 \tan A \sin A$$
RHS $4\sqrt{mn} = 4\sqrt{(\tan A + \sin A)(\tan A - \sin A)}$

$$=4\sqrt{\tan^2 A - \sin^2 A}$$

$$=4\sqrt{\frac{\sin^2 A - \sin^2 A \cos^2 A}{\cos^2 A}}$$

$$=4\sqrt{\frac{\sin^4 A}{\cos^2 A}}$$

$$=4\frac{\sin^2 A}{\cos^2 A}$$

$$= 4 \tan A \sin A$$

$$\therefore m^2 - n^2 = 4\sqrt{mn}$$