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- Q-1. The number of surjections from A = 1,2, ... n ,  $n \ge 2$  onto B = (a, b) is
- (a)  $nP_2$
- (b)  $2^n 1$
- (c)  $2^n + 1$
- (d) none of these
- Q-2. Set A has 3 elements and set B has 4 elements. The number of injection that can be defined from A to B is
- (a) 144
- (b) 12
- (c) 24
- (d) 64
- Q-3.  $f: R \to R$  is a function defined by f(x) = 10x 7. if  $g = f^{-1}$ , then g(x) = 10x 7.
- (a)  $\frac{1}{10x-7}$
- (b)  $\frac{1}{10x+7}$
- (c)  $\frac{x+7}{10}$
- (d)  $\frac{x-7}{10}$
- Q-4. The number of objective function from set A to itself when A contains 106 elements is
- (a) 106
- (b)  $(106)^2$
- (c) 106!
- (d) 2<sup>106</sup>
- Q-5.  $f(x) = |\sin x|$  has an inverse if its domain is
- **(**a**)** [0, π]
- (b)  $\left[0, \frac{\pi}{2}\right]$  (c)  $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$

- (d) none
- Q-6. If the area of the triangle formed by points z, iz and z + iz is 50 square units, then |z| is
- (a) 5
- (b) 10
- (c) 15
- (d) none of these
- Q-7. if area of triangle on plane turned by number z,  $\omega z$  and  $z + \omega z$  is  $4\sqrt{3}$ , then |z| is
- (a) 4
- (b) 2
- (c) 6
- (d) 3
- Q-8. The locus of point z satisfying  $\operatorname{Re}(\frac{1}{z}) = k$ , when k is a non-real real number is
- (a) Straight line
- (b) A circle
- (c) An ellipse
- (d) A hyperbola
- Q-9. The locus of point z satisfying  $Re(z^2) = 0$  is
- (a) Point of straight lines
- (b) Circle
- (c) Hyperbola
- (d) None of these
- Q-10. If  $a_1, a_2, a_3$  are in G. P with common ratio r, then value of  $a_3 > 4a_2 3a_1$  holds if
- (a) 1 < r < 3
- (b) -3 < r < -1
- (c) r < 3 or r < 1
- (d) none of these
- Q-11 Let a, b, c be in A. P. and |a| < 1, |b| < 1, |c| < 1.

If 
$$x = 1 + a + a^2 + ... \infty$$

$$y = 1 + b + b^2 = \dots \infty$$

$$z = 1 + c + C^2 = \dots \infty$$

Then x, y, z are in

- (a) A. P
- (b) G. P
- (c) H.P

- (d) None
- Q-12. Let  $S \subset (0, \pi)$  denotes set of values of x.

If 
$$8^{1+|\cos x|+\cos^2 x+|(\cos^3)x|} + \dots = 4^3$$
, then  $s = 1$ 

- (a)  $\frac{\pi}{2}$
- (b)  $(\frac{\pi}{3}, \frac{2\pi}{3})$
- (c)  $(-\frac{\pi}{3}, \frac{2\pi}{3})$
- (d)  $(\frac{\pi}{3}, \frac{2\pi}{3})$
- Q-13. If  $\log_x a, a^{\left(\left(\frac{x}{2}\right)\right)}$  and  $\log_x b$  are in G. P. then x is equal to
- (a)  $\log_a (\log_b a)$
- (b)  $\log_a(\log a)$
- (c)  $-\log_a(\log_a b)$
- (d)  $\log b$
- Q-14. IF  $a \in z$ , (x a)(x 10) + 1 = 0 has integral roots, then values of a are
- (a) 10,8
- (b) 12,10
- (c) 12,8
- (d) none
- Q-15. If  $(3x)^2 + (27x3^{1 p} 15)x + 4 = 0$  has equal roots, then p is equal to
- (a) 0
- (b) 2
- (c)  $-\frac{1}{2}$
- (d) None
- Q-16. The value of a for which  $(1-2a)x^2-6ax-1=0$  and  $ax^2-x+1=0$  have at least one root, in common are
- (a) 0,  $-\frac{1}{2}$
- (b)  $\frac{1}{2}, \frac{2}{9}$
- (c)  $\frac{2}{9}$
- (d)  $0, \frac{1}{2}, \frac{2}{9}$
- Q-17. There are m copies of each n different books in libaray. The number of ways in which one or more than one book can be selected as
- (a)  $m^n + 1$
- (b)  $(m+1)^n 1$

- (c)  $(n+1)^n m$
- (d) "

Q-18. The number of ways in which one or more balls. can be selected out of 10 white, 9 green and 7 blues balls, is

- (a) 892
- (b) 881
- (c) 891
- (d) 879

Q-19. The number of all 3 elements subsets of det  $(a_1, a_2, a_3 ... a_n)$  which contains  $a_i$  is

- (a)  $nC_3$
- (b)  $n 1C_3$
- (c)  $n 1C_2$
- (d) None of these

Q-20. The number of terms which are free from radical signs in expansion

$$(y^{(\frac{1}{5})} + (x^{(\frac{1}{10})}))^{55}$$
 is

- (a) 5
- (b) 6
- (c) 7
- (d) None of these

Q-21. If sum of coefficient of  $(a + b)^n$  is 4096, then greatest coefficient is

- (a) 924
- (b) 792
- (c) 1594
- (d) None of these

Q-22.  $_{3rd}$  term in the expansion of  $\left(\frac{1}{x} + \left(x^{\log_{10} x}\right)\right)^5$  x > 1 is 1000, then x is

- (a) 100
- (b) 1000
- (c) 1
- (d)  $\frac{1}{\sqrt{10}}$

Q-23. If A is square matrix of order n, then adj (adj A) is equal to

- (a)  $|A|^n A$
- (b)  $|A|^{n-1}A$
- (c)  $|A|^{n-1}A$

- (d)  $|A|^{n-3}A$
- Q-24. If A is singular, then A adj A is matrix
- (a) Identify
- (b) Null
- (c) Scalar
- (d) None of these
- Q-25. If  $A = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$  and  $n \in \mathbb{N}$ , then  $A^n$  equals
- (a)  $2^{n}A$
- (b)  $2^{n-1}A$
- (c) nA
- (d) None of these

Q-26. If 
$$\begin{vmatrix} x^n & x^{n+2} & x^{n+3} \\ y^n & y^{n+2} & y^{n+3} \\ Z^n & Z^{n+2} & Z^{n+3} \end{vmatrix} = (x-y) (y-z) (z-x) (\frac{1}{x} + \frac{1}{y} + \frac{1}{z})$$
, then n equals

- (a) 1
- (b) -1
- (c) 2
- (d) -2
- Q-27. The orthocenter of the triangle formed by lines xy = 0 and x + y = 1 is
- (a)  $(\frac{1}{2}, \frac{1}{2})$
- (b)  $(\frac{1}{3}, \frac{1}{3})$
- (c) (0,0)
- (d)  $(\frac{1}{4}, \frac{1}{4})$
- Q-28. The area of figure formed by  $ax \pm by \pm = 0$  is
- (a)  $\frac{C^2}{ab}$
- (b)  $\frac{2C^2}{ab}$
- (c)  $\frac{C^2}{2ab}$
- (d) None of these
- Q-29. The equation  $ax^2 + by^2 + cx + cy = 0$  represent pair of lines if
- (a) c = 0
- (b) a + b = 0
- (c) c = 0 or a + b = 0
- (d) None of these

Q-30. If an equilatual triangle is inscribed in circle  $x^2 + y^2 = a^2$ , then length of each side is

- (a)  $\sqrt{2a}$
- (b)  $\frac{\sqrt{3}}{2}a$
- (c)  $\sqrt{3}$  a
- (d) None of these

Q-31. The lotus rectum of parabola whose focal chord is P S Q is such that SP = 3 and SQ = 2 is given by

- (a)  $\frac{24}{5}$
- (b)  $\frac{12}{5}$
- (c)  $\frac{6}{5}$
- (d) None of these

Q-32. Find c such that straight line y = 4x + c touches curve  $\frac{x^2}{4} + y^2 = 1$  is

- (a) 0
- (b) 3
- (c) 2
- (d) Infinite

Q-33. The eccentricity of the conic represented by  $x^2 - y^2 - 4x + 4 + 4y + 16 = 0$ is

- (a) 1
- (b)  $\sqrt{2}$
- (c) 2
- (d)  $\frac{1}{2}$

Q-34. If f(x + 2y, x-2y) = xy, then f(x, y) equal

- (a)  $\frac{x^2 y^2}{8}$
- (b)  $\frac{x^2 y^2}{4}$
- (c)  $\frac{x^2 + y^2}{2}$
- (d)  $\frac{x^2 y^2}{2}$

Q-35. The period of f (x) =  $\sin^4 x + \cos^4 x$  is

- (a)
- (b)  $\frac{\pi}{2}$
- (c) 2π
- (d) None of these

- Q-36.  $\lim_{x\to 0} \frac{\sqrt{x^2+1}-1}{\sqrt{x^2+9}-3}$  is equal to
- (a) 3
- (b) 4
- (c) 1
- (d) 2
- Q-37.  $\lim_{x\to 0} \left( \left( \frac{x+5}{x-1} \right) \right)^x$  is equal to
- (a)  $_{e^6}$
- (b) e<sup>5</sup>
- (c) e
- (d) 1
- Q-38. If  $f(x) = \sin^{-1}(\frac{2x}{1+x^2})$ , then f(x) is differentiable on
- (a) [-1,1]
- (b) R-[-1,1]
- (c) R- (-1,1)
- (d) None of these
- Q-39. If  $f(x) = |x a|\phi(x)$  is continuous, then
- (a)  $f'(a+) = \phi(a)$
- (b)  $f'(a) = -\phi(a)$
- (c)  $f'(a^+) = \phi'(a^{-1})$
- (d) None of these

Q-40. If 
$$f(x) = \sqrt{x^2 + 9}$$
 then  $\lim_{x\to 0} \frac{f(x) - f(4)}{x - 5}$  equals

- (a)  $\frac{5}{4}$
- (b)  $-\frac{4}{5}$
- (c) <sub>4/5</sub>
- (d) None of these